Massachusetts Institute of Technology

Spring Term 2005

8.02X Electricity and Magnetism

Practice-Quiz #4b

So(a hous

Problem 1 (25 points)

In the HVPS experiment, you built a "transformer" by winding 6 loops of wire around a tightly wound red coil.

(a) Which side of the transformer was the primary side in this setup? The 6 Loops

(b) Assume that in your setup the inner (red) coil had length L_1 , number of windings N_1 and radius R_1 . The outer coil (wire loops) had length L_2 , number of windings N_2 and radius R_2 . Derive an expression for the mutual inductance of the two coils. Show work!

- (c) Based on the known output voltages of LVPS and HVPS, estimate (within a factor of 2) a numerical value for the number of windings of the red coil (ignore the different length for primary and secondary coil).
- (d) Assume a current $I_2(t) = I_0 * \cos(\omega t)$ was flowing through the outer coil. What would the voltage across the red coil $\Delta V_1(t)$ be?

b)
$$EMF_{COIL} = -M \frac{dI_{i}}{dt}$$

$$= -N_{2} \cdot \pi R_{i}^{2} \cdot \frac{dR_{i}}{dt} = -N_{2} \cdot \pi R_{i}^{2} \cdot \frac{M_{i}}{L_{i}} \cdot \frac{M_{0}}{dt} \cdot \frac{dI}{dt}$$

$$() \quad V_{LVPS} \approx 10U \quad V_{LVPS} = N_{LVPS} \approx 6$$

$$V_{HVPS} \approx 10V \quad V_{HVPS} = N_{HVPS} \approx 6000$$

$$M_{HVPS} \approx 100V \quad V_{HVPS} = N_{HVPS} \approx 6000$$

Problem 2 (25 points)

Shown below is a circuit that is connected to a DC power supply with an output voltage V_0 . For times t < 0, the switch is in position 1 and a current is flowing through the inductor (inductance L), the resistor (resistance R) and the power supply. Assume the switch has been closed for a very long time and the resistance of the inductor is negligible. Assume also that for t < 0, the capacitor (Capacity C) is discharged (Q=0).

At t=0, the switch is moved to position 2 and the power supply and resistor are therefore removed from the circuit.

- (a) At t=0, what is the total energy stored in the circuit formed
- corresponds to the circuit formed by the inductor and capacitor (after t=0). Identify which elements in the mechanical system correspond to which circuit elements.

Mass on a spring: Incubie: Mass to Inductor Restaving Force: Spring to Capacitor (c) How will the charge Q(t) on the capacitor vary with time? Give an equation in terms of the quantities defined above. $Q(t) = Q_0 \cdot \sin(\omega t) \quad \omega \cdot t \quad \omega = \sqrt{\frac{1}{LC}} \quad and \quad Q_0 = \sqrt{LC} \cdot I$

(d) On the graph below, sketch how the energy in the inductor varies with time after t=0.



Problem 3 (25 points)

Consider a plane wave with an amplitude that is described by the following equations:

$$A_x = 0$$

 $A_y = 0$
 $A_z = A_0 \cos(\omega t - (2\pi/3m) x)$

- (a) Which direction is the wave traveling in?
- (b) How big is the wave length of the wave?
- (c) Could these equations describe a sound wave? Explain your answer.
- (d) If the wave was electromagnetic, what would the frequency f be?

$$b) \quad \lambda = 3m$$

c) No. A is I to i -> transverse wave

d)
$$2 \cdot f = 3 \cdot 10^8 \frac{m}{s} = 7 f = 10^8 Hz$$

Problem 4 (25 points) AMP experiment

- (a) What is the purpose of the AMP experiment? (1-2 sentences)
- (b)How did you calibrate the AMP setup? What does the calibration curve tell you? (2-3 sentences)
- (c) Shown below is a calibration circuit like that on the AMP experiment. All voltages a measured relative to the common line C, which is defined as 0V. What is the voltage at point X when the slider of the potentiometer is 1/2 way between the extreme positions?
- (d)What are the maximum and minimum voltages at point D relative to C, when the slider is moved from one extreme position to the other?



a) Purpose: To "amplify" the input college,
i.e. creak an output signal that is proportional
to the input, but larger a factor "g", the gain.
b) First should the input and zeroed the
output using 100 h R pat, with HMM on
the 250 mb setting. Then connected calibration
odport and to Input A. Vary Input college
from - 67 mb to 67 mb and record output
voltage as a function of lapart voltage.
c) By Symmetry V(x) = O
d) Equivalent cliagram
A QOU

$$R_1 = (\frac{1}{1.34R} + \frac{1}{544R})^{-1} \approx 14.R$$

 $R = 914R$
 $R = 14R$
 $R = 14R$
 $R = 160 \text{ cm}^{-1} = 14.R$
 $R = 160 \text{ cm}^{-1} = 14.R$
 $R = 160 \text{ cm}^{-1} = 16.R$
 $R = 160 \text{ cm}^{-1} = 16.R$