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## Biomaterials - Tissue Interactions

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### Homework #8

#### New hypothetical mechanism for tissue regeneration by a collagen-GAG scaffold

It has recently been observed that TGF $\beta$ 1 binds extensively on the large surface of a highly porous collagen-GAG scaffold. It will be assumed that bound TGF $\beta$ 1 is unavailable for regulation of cell function and that only unbound, or “free”, TGF $\beta$ 1 is involved in cell regulation. You are a researcher exploring the consequences of this new finding with the objective of using this fact in the design of new biomaterials-based approaches to regeneration.

A. The researcher is familiar with data (“contraction-blocking data”) showing that collagen-GAG scaffolds block wound contraction most effectively when the average pore size lies between approximately 20 and 140  $\mu\text{m}$ . See Fig. 1. Having conducted preliminary studies you have found out that the mass of bound TGF $\beta$ 1,  $\mathbf{m}$ , is directly proportional to the specific surface,  $\sigma$ , of a series of scaffolds.

$$\mathbf{m} = \mathbf{C}\sigma$$

where  $\mathbf{C}$  is a constant of proportionality. The specific surface,  $\sigma$ , of scaffolds is known to depend on the pore size,  $\mathbf{d}$ , by the following relation (Gibson and Ashby, 1997):

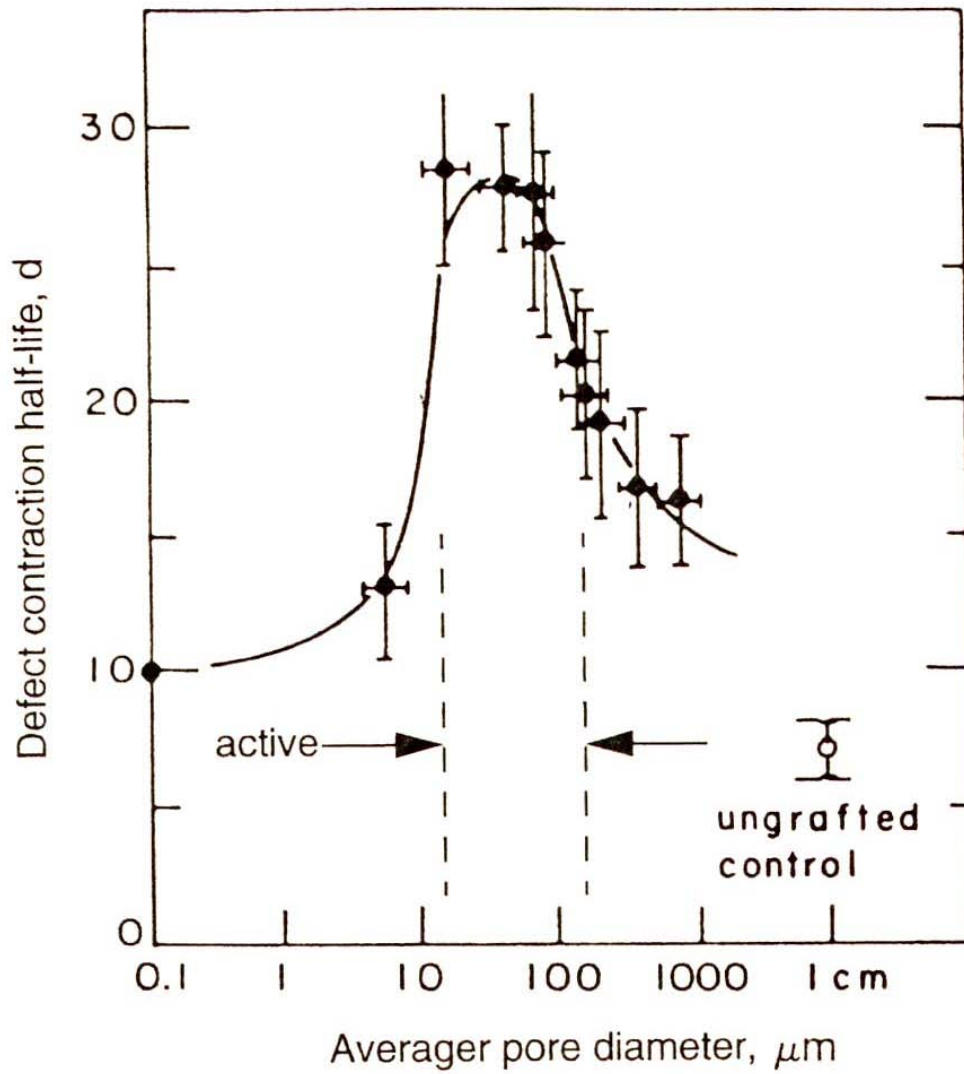
$$\sigma = \mathbf{K}/\mathbf{d}$$

where  $\mathbf{K}$  is a constant of proportionality. Write the relation between the mass of bound TGF $\beta$ 1,  $\mathbf{m}$ , and the average pore size,  $\mathbf{d}$ , of a series of scaffolds.

B. Collagen-GAG scaffolds degrade during implantation. Set up and solve a linear differential equation with one or more constant coefficients which can be used as a model to describe the decay of the mass of bound TGF $\beta$ 1,  $\mathbf{m}$ , with time of implantation. Assume that the mass of bound TGF $\beta$ 1,  $\mathbf{m}$ , is directly proportional to  $\mathbf{M}$ , the total scaffold mass.

C. Describe briefly the hypothetical role that extensive binding of TGF $\beta$ 1 on the scaffold surface plays in scaffold- induced organ regeneration. Describe one or a small number of measurements, conducted in vivo, that could be used to test the validity of such a mechanism.

D. Study the “contraction-blocking data” in Fig. 1. Can the entire set of these data be explained by the relation you have derived above between  $\mathbf{m}$  and  $\mathbf{d}$ ? Explain briefly.



**Figure 1: Yannas et al. 1989**

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Source: Yannas, I., et al. "Synthesis and Characterization of a Model Extracellular Matrix that Induces Partial Regeneration of Adult Mammalian Skin." *PNAS* 86 (1989): 933-937.

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